

STANDARD ERROR, CENTRAL LIMIT THEOREM (10/31/19)

Read: DD (A) chpt 1-3 Take Home Midterm due
(B) chpt 1-10 Sun Night 10 Nov 19

LN pg 1-136

DD extra office hours for midterm
daily starting Mon

HW 2 due tonight

$$\frac{100\%}{60} = 10 \text{ hours}$$

$$= P_F(S' > \$10)$$

$P_F(\text{coming out ahead after 1000 \$1 bets on single #}) = ?$
Frequentist

2 WAYS

① math (1710)

(since 1950)

② computer simulation formula (2)

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$$\left(\begin{array}{l} \text{expected} \\ \text{value of } S' \end{array} \right) = \text{EV of } S' = E_{\text{IID}}(S') = ?$$

Math
FACT

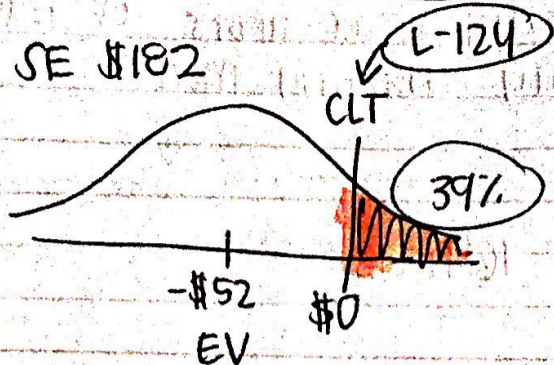
$$E_{\text{IID}}(S') = \left(\begin{array}{l} \# \text{ of} \\ \text{draws} \end{array} \right) \left(\begin{array}{l} \text{pop} \\ \text{mean} \end{array} \right) = n/M$$

$(1000)(-0.05)$
↓

$$E_{IID}(-S) = -\$52$$

Utility (1730)

SE \$182



long run
hist of S'

After $n=1000$

\$1 bets on single #,
you expect to have won

~~ANS~~

$$+0.29 = \frac{(\$10) - (-\$52)}{\$182}$$

de Moivre
(1710)

(EV of sum) = $nM = -\$52$, give or take about

(standard error of S') = (SE of $-S'$) = $SE_{IID}(-S) = ?$

Math fact

$SE_{IID}(-S) = S'$ is (noisy) uncertain; $SE_{IID}(S)$ represents how much uncertainty (noise) we have about S'

~~signal~~

signal
information ↑

uncertainty
noise ↓

\bar{y} is uncertain b/c $\bar{y} = (y_1 + \dots + y_n)$ and each of the y_n is uncertain

The pop SD σ represents how much uncertainty we have about each of the y_n

~~signal~~

as $\sigma \uparrow$

$SE_{IID}(\bar{y}) \uparrow$

N X
M X
 $\sigma \uparrow$
n \uparrow
M X

$SE_{IID}(\bar{y}) \uparrow$

~~SE~~

$$SE_{IID}(\bar{y}) = \sigma \sqrt{n} = (\$5.70) \sqrt{1000} = \$182$$

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