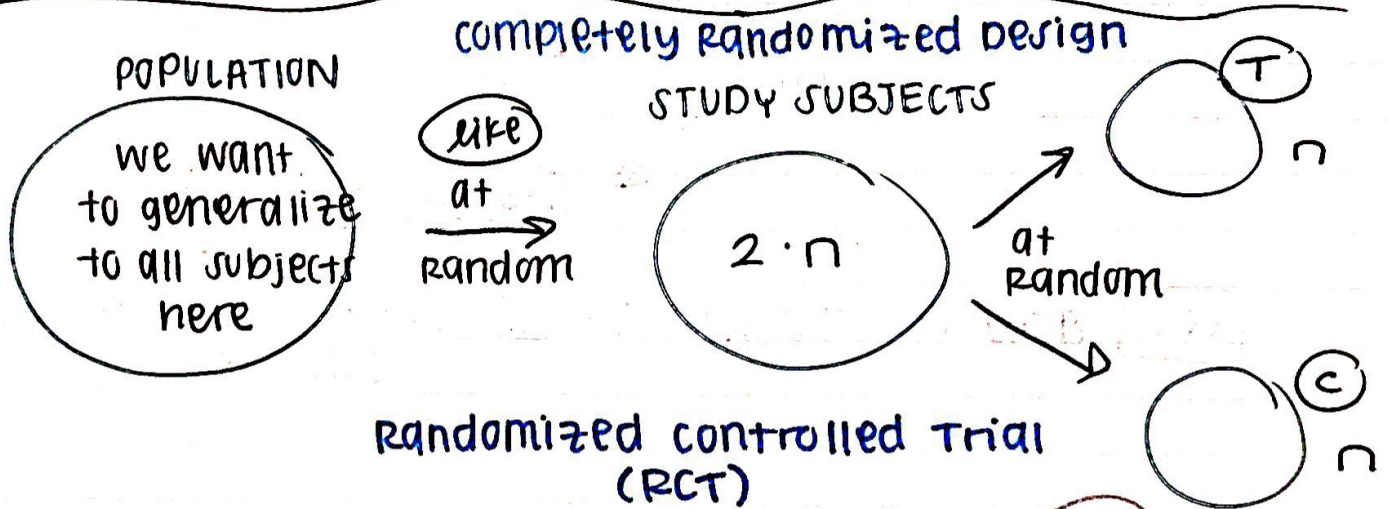


# DESIGN & PROBABILITY (10/22/19)

Reed: DD  
(A) chpt 1-3  
(B) chpt 1-8

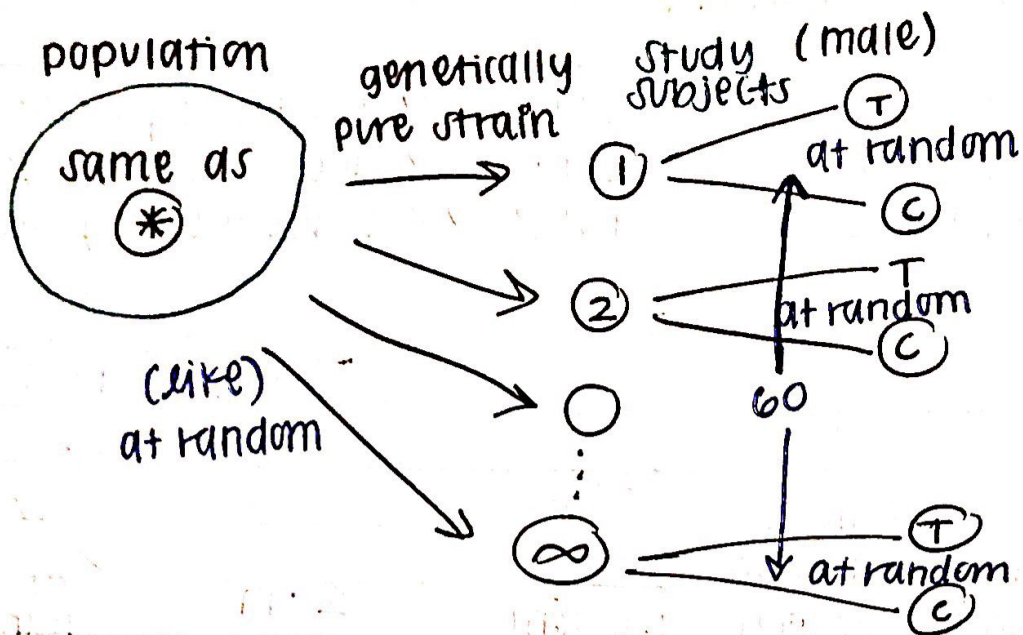
Quiz 3 → due Friday night 25<sup>th</sup> Oct  
Quiz 4 → due Tuesday night 29<sup>th</sup> Oct  
HW 2 → due Wednesday night 30<sup>th</sup>



## DEFINITION

An experimental design is valid if its unbiased. (L-77)

Q: RCT valid?  
A: yes (CRD)



Q: ~~Does~~ Do changes in  $\bar{X}$  cause changes in  $\bar{Y}$ ?  
(effect)

$Z_i$ : potential confounding factor (PCF)

here  $Z_i = \underline{\text{genetics}}$

Definition

$Z_i$  is a PCF if and only if

(a)  $Z_i, \bar{Y}$  could be associated

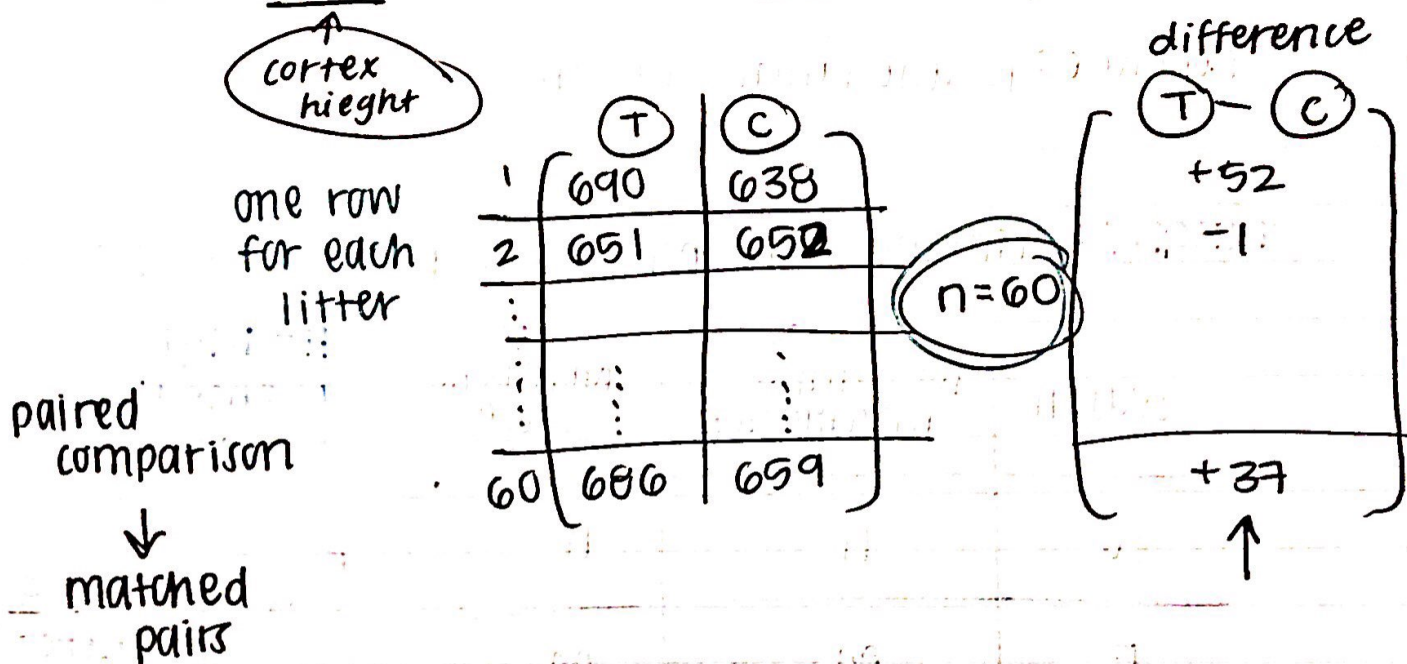
(b)  $Z_i, \bar{X}$

How to: defeat a PCF

Hold it constant

2 moments to achieve this defeat:

- ① at design time    ② at analysis time



Q<sub>1</sub>: is this paired comparison design valid?

A<sub>1</sub>: Yes, its unbiased

Q<sub>2</sub>: is paired design likely to be more accurate than CRD?

Kill PCF by hoping randomization bar made (T), (C) groups similar on PCF this will happen high probability

A<sub>2</sub>: Yes, because paired design kills PCF by holding it constant

New Question: If  $\bar{x}$ ,  $\bar{y}$  associated, is it always time that either  $\bar{x}$  is causing  $\bar{y}$  or  $\bar{y}$  is causing  $\bar{x}$

$\bar{x} \rightarrow \bar{y}$

$\bar{x} \leftarrow \bar{y}$

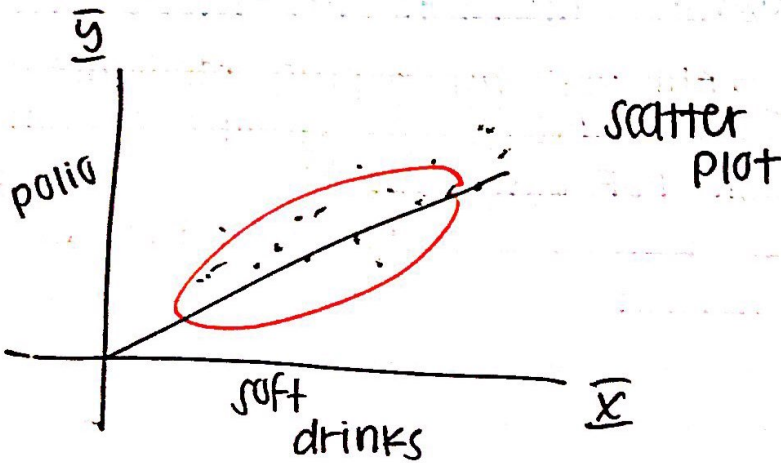
Rephrase: is association = causation?

THEORY: drinking soda pop causes polio to be spread

season	$\bar{x}$ soft drink consumption	$\bar{y}$ new polio cases
Su	H	H
F	M	M
W	L	L
Sp	M	M

H = high  
M = medium  
L = low

Q: Are  $\bar{x}$ ,  $\bar{y}$  associated?  
A: yes



association is (+)

Q: does this prove that  $\bar{x}$  causes  $\bar{y}$ ?

A: no; this story was wrong

association  $\neq$  causation

$\leq$  ← weaker than or equivalent to

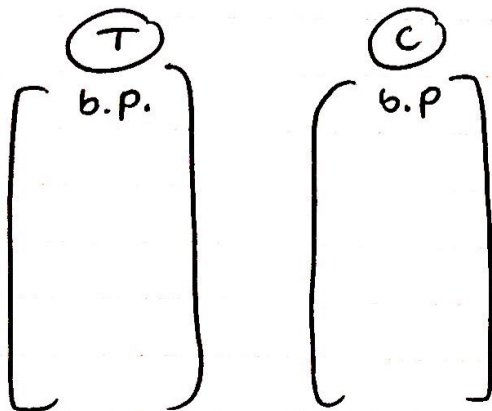
Q: why isn't assoc. = causation?

A: PCFs

CASE STUDY **R-35** : The contraceptive drug study

outcome $\bar{y}$	treatment $\bar{x}$
blood pressure	1 = pill use (T) 0 = not (C)

if obs. study,  
then worry a lot  
about PCFs



mean  
SD  
Histogram

mean  
SD  
Histogram

(2) **age** is a PCF

age  $\uparrow$  b.p.  $\uparrow$  ✓  
age  $\uparrow$  b.p.  $\downarrow$  ✓

If we don't hold age constant  
("control for the PCF ( $Z_1 = \text{age}$ ")  
this will bias results to make pill  
look less harmful than it really is

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After controlling for age, pill use associated w/  
5mmHg increase in systolic b.p.

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**Q:** Is this difference practically significant?

**A:** No if short (time) pill use; yes if long use